

# S10 Unit B: Physics:

## Conservation of Energy

Name: \_\_\_\_\_

Date: \_\_\_\_\_

### Recall the Energy Eqns:

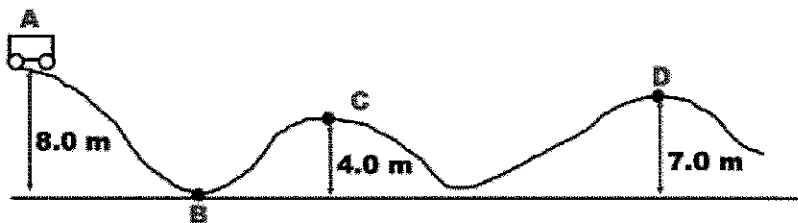
$$E_p = mgh$$

$$E_k = \frac{1}{2}mv^2$$

### The Conservation of Energy States:

*Energy cannot be created or destroyed, only changed in form.*  
or  
*The total energy a system is always the same.*

ex) A roller coaster ( $m = 100 \text{ kg}$ ) starts from rest at point **A**, as shown below.



a) Determine the energy of the roller coaster at point **A**.

$$E_p = mgh$$

$$E_p = (100 \text{ kg})(9.81 \text{ m/s}^2)(8.0 \text{ m})$$

$$E_p = 7848 \text{ J}$$

$$E_p = \underline{7.8 \times 10^3 \text{ J}}$$

At point **A** all of the energy is potential energy as the coaster isn't moving. So we just find the gravitational potential energy.

b) Determine the speed of the roller coaster at point **B**.

$$E_k = \frac{1}{2}mv^2$$

$$7.8 \times 10^3 \text{ J} = \frac{1}{2}(100 \text{ kg})v^2$$

$$7.8 \times 10^3 \text{ J} = 50v^2$$

$$156 = v^2$$

$$v = \underline{12 \text{ m/s}}$$

At point **B** all of the energy is kinetic energy, but the total energy stays the same as at point **A** by the conservation of energy. So, the energy is the same as the last part of the question and we just solve for speed.

c) Find the speed at point **C**.

$$7.8 \times 10^3 \text{ J} = E_p + E_k$$

$$7.8 \times 10^3 \text{ J} = (100 \text{ kg})(9.81 \text{ m/s}^2)(4.0 \text{ m}) + \frac{1}{2}(100 \text{ kg})v^2$$

$$7.8 \times 10^3 \text{ J} = 3924 \text{ J} + 50v^2$$

$$3876 \text{ J} = 50v^2$$

$$v = \underline{8.8 \text{ m/s}}$$

At point **C** the total energy is still equal to  $7.8 \times 10^3 \text{ J}$  (left side of equation), but it is now made up of potential and kinetic energy (right side of equation). So the total energy is equal to the sum of  $E_p$  and  $E_k$ .

# Conservation of Energy Practice Questions

Show all work to receive full marks.

1. Using the diagram on the previous page, determine the speed of the roller coaster at point D. (2 marks)

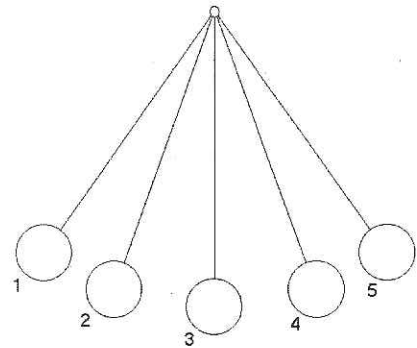
$$\begin{aligned}
 7.8 \times 10^3 \text{ J} &= E_p + E_k \\
 7.8 \times 10^3 \text{ J} &= mgh + \frac{1}{2} m \vec{v}^2 \\
 7.8 \times 10^3 \text{ J} &= (100 \text{ kg})(9.81 \text{ m/s}^2)(7 \text{ m}) + \frac{1}{2} (100 \text{ kg}) \vec{v}^2 \\
 7.8 \times 10^3 &= 6867 + 50 \vec{v}^2 \\
 -6867 & \quad -6867 \\
 933 &= 50 \vec{v}^2 \\
 \sqrt{\vec{v}^2} &= \sqrt{18.66} \quad \vec{v} = \underline{\underline{4.3 \text{ m/s}}}
 \end{aligned}$$

2. A baseball is thrown vertically upwards with a speed of 15.0 m/s. How high will the baseball go before it stops? (2 marks)

$$\begin{aligned}
 E_k &= E_p \\
 \frac{1}{2} m \vec{v}^2 &= mgh \\
 \frac{1}{2} \vec{v}^2 &= gh \\
 \frac{1}{2} (15 \text{ m/s})^2 &= (9.81 \text{ m/s}^2) h \\
 \frac{112.5}{9.81} &= \frac{9.81 h}{9.81} \\
 h &= \underline{\underline{11.5 \text{ m}}}
 \end{aligned}$$

3. Describe the energy changes the pendulum to the right goes through as it starts at position 1, moves to position 3 and stops at position 5. (3 marks)

$$\begin{aligned}
 \textcircled{1} \quad E_p &\rightarrow E_k \\
 \textcircled{3} \quad E_k &\rightarrow E_p \\
 \textcircled{5} \quad E_p &\rightarrow E_k
 \end{aligned}$$



4. Tarzan is running at a speed of 3.5 m/s and grabs a long vine that is hanging vertically from a tree. How high can the ape-man swing? (2 marks)

$$\begin{aligned}
 E_k &= E_p \\
 \frac{1}{2} m \vec{v}^2 &= mgh \\
 \frac{1}{2} (3.5 \text{ m/s})^2 &= (9.81 \text{ m/s}^2) h \\
 h &= \underline{\underline{0.62 \text{ m}}}
 \end{aligned}$$